

# python求解二元二次方程组\_【CTF WriteUp】2020祥云杯 Crypto题解

原创

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【线下混战结束, 终于有时间整理WP了】

Crypto

Exposure

本题为已知dp部分高位的情况, 使用通过化简构造f(x)的Coppersmith解决

```
from sage.all import *
```

```
n =  
1403760491349348221539642434030312019222395880541333190564834133119633853212796821863549
```

```
e = 7621
```

```
c =  
4673596220485719052047643489888100153066571815569889888260342202348499838866885869291225
```

```
s =  
1153696846823715458342658568392537778171840014923745253759529432977932183322553944430236
```

```
def coppersmith(bits, k):
```

```
F. = PolynomialRing(Zmod(n))
```

```
invE = inverse_mod(e, n)
```

```
f = (s << bits) + x + (k - 1) * invE # make monic
```

```
x0 = f.small_roots(X=2 ** bits, beta=0.44, epsilon=1/32)
```

```
return x0
```

```
for k in range(1, e):
```

```
bits = 200
```

```
x0 = coppersmith(bits,k)
```

```
if len(x0) != 0:
```

```
x = Integer(x0[0])
```

```
dp = x + (s << bits)
```

```

p = (e*dp - 1) // k+1
if p != -1:
q = n // p
assert n == p * q
phi = (p-1)*(q-1)
d = inverse_mod(e,phi)
print d
print pow(c,d,n)
more_calc

```

本题怎么说呢。。网上充满了非预期解，因为这题实在太容易非预期了，主代码又肯定不能跑，试一试就出来了。所以这里我们讲一讲正规套路。本题改编自2012年新加坡数学奥林匹克。

题目要求计算

的值。注意到当  $i = 1, 2, \dots, (p-1)/2$  时，

所以

其中最后一步根据费马小定理，对于素数  $p$  与小于  $p$  的数  $i$ ，有  $i^{p-1} \equiv 1 \pmod{p}$ 。注意到

从意义上代表从  $p$  个元素中取出偶数个元素的方法。由于  $p$  是奇数，所以从  $p$  个元素中取出偶数个元素的方法数 = 从  $p$  个元素中取出奇数个元素的方法数(剩下)，且二者之和为从  $p$  中取出元素的方法数  $2^{p-1}$ 。由于没有计算取出 0 个元素的情况，所以此处有

即

以此方法求出  $q$ ，进而求解本题。完整代码如下：

```

#!/usr/bin/env python
# -*- coding: utf-8 -*-
import gmpy2
from libnum import n2s
e = 65537
p =
2740510704175326648914538862185816951187299662276526706486854211726987553136493989667166

```

```
c =
3505591868374888328217478432365181356052073760318580022742450042876226493302151138187199
```

```
s = p - (pow(2, p, p*p)-2)//p
```

```
q = gmpy2.next_prime(s)
```

```
n = p*q
```

```
e = 0x10001
```

```
phi = (p-1)*(q-1)
```

```
d = gmpy2.invert(e, phi)
```

```
print n2s(pow(c, d, n))
```

RSAssss

n是四个数的乘积，先yafu分解一下试试，得到两个值

```
a =
8961506852753883631560212415400830028663693459961733486750905307662271536580937174003731
```

```
b =
8961506852753883631560212415400830028663693459961733486750905307662271536580937174003731
```

再往下分解不下去了，所以这两个应该分别是  $p * \text{next\_prime}(q)$  和  $q * \text{next\_prime}(p)$ 。注意到  $\text{next\_prime}(p)$  有一个性质，就是当  $p$  较大时，并不会完整验算，所以  $\text{next\_prime}(p) - p$  实际上很小。设

$$\text{next\_prime}(q) - q = x$$
$$\text{next\_prime}(p) - p = y$$

当  $x$  与  $y$  已知时， $p*(q+x) = a$  和  $q*(p+y) = b$  构成二元二次方程组，可以通过爆破  $x$  与  $y$  尝试解方程，在正整数范围内求出解即为  $p$  和  $q$  之一。完整解题代码如下：

```
#!/usr/bin/env python
```

```
# -*- coding: utf-8 -*-
```

```
import gmpy2
```

```
from libnum import n2s
```

```
n =
8030860507195481656424331455231443135773524476536419534745106637165762909478292141556846
```

```
c =
3304124639719334349997663632110579306673932777705840648575774671427424134287680988314129
```

```
a =
8961506852753883631560212415400830028663693459961733486750905307662271536580937174003731
```

```

b =
8961506852753883631560212415400830028663693459961733486750905307662271536580937174003731
< | III | >
for x in range(1, 1000):
for y in range(1, 1000):
delta = (a-b-x*y)**2 + 4*a*x*y
tmp = gmpy2.iroot(delta, 2)
if(tmp[1]):
p = (a-b-x*y + int(tmp[0])) / (2*x)
if (a*b)%p == 0:
print p
pp = gmpy2.next_prime(p)
print pp
tn = n // (p*pp)
tq = int(gmpy2.iroot(tn,2)[0])
qq = gmpy2.next_prime(tq)
q = tn // qq
print q
print qq
print n - p * pp * q * qq
phi = (p-1) * (q-1) * (pp-1) * (qq-1)
d = gmpy2.invert(0x10001, phi)
print n2s(pow(c,d,n))
simpleRSA

```

根据代码，我们可以发现n很大，但是是三个数pqr的乘积，简单测试发现常规wiener脚本和boneh-durfee脚本均不可用，需要深入理解算法的原理。百度搜索wiener攻击，发现这样一种解释：

首先引入一个概念：连分数。对于任意两个正整数a、b，我们尝试构造这样一个分数的序列：

使其不断接近a/b。存在这样一种构造方法，即首先将a/b完整展开为繁分数形式，然后每次计算其中的一部分逐渐逼近a/b。举一个简单的例子，例如a=11369, b=31337

(Word公式编辑器只能写10层，这俩破数选的真不好。。)

我们将最后的分数部分去掉，生成这样一个数列：

这就是一个逐渐逼近，并最终达到 $a/b$ 的连分数序列。

接下来回到题目。题目满足基础等式

所以

来看一下各自的大小：pqr各1024位，所以n是3072位左右； $\phi(n)$ 和e也差不多；d是512位；根据算式可知k也差不多，所以原式变为

注意到 $\phi(n)$

二者差距是很小的，所以结论是 $e/n$ 与 $k/d$ 相差无几。

wiener算法的强大之处在于，wiener本人证明了在 $e/n$ 的连分式展开中，必定有一个是 $k/d$ 。本题我们也采用相同的方式展开，找到其中512位的那一项即为d，求即 $\text{pow}(c, d, n)$ 解出明文。完整代码如下：

```
#!/usr/bin/env python
# -*- coding: utf-8 -*-
from libnum import n2s

def continuedFraction(x, y):
    ret = []
    while y:
        ret.append(x / y)
        x, y = y, x % y
    return ret

def expand(ctnf):
    _ctnf = ctnf
    _ctnf.reverse()
    numerator = 0
    denominator = 1
    for x in _ctnf:
        numerator, denominator = denominator, x * denominator + numerator
    return (numerator, denominator)

def progressiveFraction(x, y):
```

```

cfe = continuedFraction(x, y)

cfeL = len(cfe)

ret = []

for i in xrange(1, cfeL):

ret.append(expand(cfe[0 : i]))

return ret

e =
1072295425944136507039938677101442481213519408125148233880442849206353379681989305000570
< [REDACTED] >

n =
1827221992692849179244069834273816565714276505305246103435962887461520381709739927223055
< [REDACTED] >

c =
1079929174110820494059355415059104229905268763089157771374657932646711017488701536460687
< [REDACTED] >

s = progressiveFraction(e, n)

for i in s:

if len(bin(i[0]))-2 == 256:

print n2s(pow(c,i[0],n))

easy matrix

(第二天没打，直接搬运)

```

解题方法是利用Babai's Nearest Plane算法计算CVP，再构造格解决

解题代码来源：Gm1y大佬的博客

祥云杯2020 Crypto wp

```

from sage.modules.free_module_integer import IntegerLattice

```

```

row = 128

```

```

prime = 2129

```

```

column=42

```

```

ma=[[133, 210, 141, 293, 30, 290, 445, 377, 292, 201, 92, 68, 374, 169, 69, 70, 195, 495, 32, 361, 202, 158,
198, 187, 95, 449, 447, 507, 315, 475, 97, 271, 339, 123, 121, 279, 41, 341, 280, 325, 24, 293, 467, 19, 59,
284, 488, 349, 188, 373, 240, 115, 50, 173, 270, 82, 157, 398, 393, 376, 365, 228, 425, 502, 375, 85, 387,
133, 450, 501, 176, 477, 340, 221, 115, 233, 451, 202, 409, 484, 418, 268, 340, 345, 134, 363, 105, 168, 385,
135, 219, 415, 488, 454, 85, 120, 215, 455, 365, 145, 249, 158, 399, 161, 344, 372, 293, 122, 275, 253, 128,
432, 326, 72, 510, 310, 137, 293, 88, 462, 471, 479, 411, 17, 141, 375, 345, 322], [22, 367, 369, 83, 326, 195,
405, 351, 235, 430, 198, 455, 495, 509, 151, 208, 171, 202, 103, 328, 449, 95, 20, 178, 288, 179, 9, 333, 60,
489, 298, 367, 326, 441, 433, 195, 197, 330, 10, 63, 358, 336, 197, 238, 424, 167, 154, 157, 63, 53, 72, 67,
363, 349, 94, 197, 184, 463, 223, 34, 295, 392, 213, 11, 303, 295, 207, 399, 370, 429, 111, 93, 257, 245, 45,
56, 27, 68, 69, 32, 24, 478, 289, 449, 82, 61, 397, 431, 103, 356, 8, 238, 316, 320, 169, 485, 368, 158, 142,

```

430, 22, 439, 100, 455, 374, 384, 449, 307, 38, 293, 215, 70, 335, 88, 94, 360, 364, 93, 178, 374, 51, 433, 447, 484, 450, 123, 313, 237], [100, 199, 503, 511, 131, 396, 425, 44, 473, 277, 42, 303, 355, 169, 61, 172, 103, 324, 57, 467, 195, 506, 186, 429, 230, 498, 242, 143, 86, 288, 149, 268, 500, 210, 261, 135, 57, 210, 469, 281, 72, 308, 502, 168, 488, 372, 49, 314, 368, 489, 475, 156, 224, 310, 219, 190, 189, 36, 388, 497, 197, 119, 19, 444, 292, 94, 9, 21, 24, 228, 413, 3, 97, 439, 52, 123, 317, 61, 371, 266, 263, 44, 32, 13, 361, 324, 490, 235, 99, 236, 408, 340, 417, 324, 299, 152, 159, 277, 124, 27, 508, 12, 268, 48, 15, 67, 47, 370, 201, 237, 81, 65, 475, 11, 291, 227, 425, 247, 365, 205, 364, 468, 511, 300, 491, 154, 404, 189], [73, 457, 149, 367, 38, 476, 160, 112, 400, 330, 370, 18, 239, 363, 213, 378, 138, 21, 510, 240, 18, 378, 485, 204, 422, 287, 241, 95, 340, 138, 349, 150, 338, 15, 248, 205, 97, 459, 92, 440, 66, 107, 124, 285, 36, 391, 12, 19, 38, 468, 374, 395, 453, 59, 136, 163, 336, 86, 386, 457, 107, 491, 70, 459, 113, 59, 432, 180, 164, 277, 456, 474, 16, 35, 272, 265, 115, 234, 418, 249, 78, 252, 135, 323, 31, 2, 486, 323, 174, 70, 443, 55, 90, 260, 231, 256, 486, 240, 284, 59, 388, 351, 430, 71, 317, 276, 93, 504, 378, 226, 507, 258, 167, 386, 85, 478, 177, 103, 42, 176, 285, 181, 98, 120, 239, 400, 71, 215], [192, 277, 52, 44, 432, 302, 58, 172, 292, 104, 482, 328, 143, 14, 1, 246, 272, 58, 331, 131, 226, 413, 168, 303, 429, 419, 453, 429, 457, 166, 248, 490, 470, 420, 97, 502, 387, 133, 58, 464, 272, 149, 438, 57, 70, 121, 86, 371, 304, 253, 160, 192, 297, 311, 254, 244, 104, 168, 81, 237, 365, 108, 58, 130, 341, 170, 243, 129, 492, 394, 17, 354, 124, 460, 124, 381, 212, 205, 141, 369, 144, 395, 32, 446, 451, 137, 458, 85, 230, 428, 364, 210, 409, 229, 41, 194, 393, 508, 497, 302, 433, 80, 412, 5, 141, 380, 190, 191, 7, 290, 492, 382, 447, 25, 158, 431, 41, 264, 307, 488, 236, 411, 133, 160, 342, 83, 162, 436], [287, 413, 405, 325, 112, 378, 41, 43, 292, 195, 263, 70, 427, 243, 306, 288, 391, 352, 92, 78, 171, 12, 119, 252, 17, 394, 486, 411, 99, 422, 92, 408, 176, 476, 420, 286, 258, 399, 439, 374, 312, 430, 118, 469, 264, 414, 341, 169, 84, 28, 10, 491, 197, 80, 111, 196, 263, 211, 198, 264, 112, 70, 34, 429, 54, 74, 316, 147, 336, 123, 81, 321, 136, 486, 277, 103, 104, 256, 92, 379, 400, 486, 295, 359, 65, 457, 51, 242, 441, 69, 448, 158, 66, 422, 354, 208, 373, 135, 78, 402, 120, 7, 461, 508, 281, 496, 313, 195, 459, 504, 466, 289, 405, 1, 23, 341, 48, 175, 411, 58, 339, 209, 509, 240, 36, 199, 379, 248], [340, 187, 50, 85, 473, 355, 19, 133, 266, 243, 1, 290, 352, 141, 30, 303, 324, 19, 380, 360, 75, 83, 426, 435, 1, 60, 129, 408, 171, 52, 439, 160, 263, 65, 236, 294, 250, 371, 270, 61, 133, 407, 212, 14, 330, 467, 59, 258, 414, 163, 40, 122, 10, 370, 424, 487, 331, 261, 76, 375, 178, 91, 424, 273, 489, 20, 382, 306, 470, 317, 395, 287, 252, 232, 430, 274, 143, 146, 242, 96, 289, 53, 312, 353, 250, 268, 180, 446, 228, 199, 508, 280, 491, 238, 124, 230, 234, 286, 180, 153, 336, 26, 316, 356, 96, 40, 286, 136, 408, 440, 266, 181, 223, 473, 341, 4, 494, 38, 172, 258, 154, 306, 34, 94, 368, 236, 452, 270], [483, 13, 49, 109, 226, 479, 40, 333, 275, 290, 110, 23, 406, 302, 178, 389, 126, 324, 221, 89, 476, 246, 98, 22, 456, 235, 8, 22, 11, 509, 8, 493, 181, 210, 196, 128, 432, 245, 255, 85, 317, 147, 91, 17, 54, 464, 498, 383, 445, 191, 461, 307, 311, 456, 508, 211, 491, 362, 88, 283, 24, 328, 143, 238, 11, 485, 108, 335, 231, 98, 391, 166, 80, 1, 174, 26, 492, 141, 60, 323, 197, 204, 262, 16, 8, 474, 501, 33, 374, 211, 50, 61, 384, 146, 372, 161, 228, 314, 181, 171, 16, 478, 357, 145, 118, 467, 363, 410, 82, 498, 215, 410, 91, 481, 402, 215, 142, 283, 374, 405, 104, 262, 171, 92, 384, 479, 22, 328], [298, 281, 454, 291, 338, 412, 372, 461, 49, 43, 497, 428, 499, 148, 244, 207, 79, 26, 216, 470, 197, 66, 286, 211, 356, 77, 276, 110, 287, 66, 86, 380, 504, 84, 372, 475, 340, 26, 339, 437, 89, 182, 491, 149, 331, 500, 371, 262, 339, 304, 453, 362, 101, 36, 270, 288, 288, 473, 107, 313, 363, 143, 475, 55, 167, 56, 33, 152, 274, 212, 309, 89, 162, 226, 274, 429, 324, 169, 371, 99, 146, 202, 177, 381, 215, 74, 120, 93, 488, 11, 114, 61, 358, 90, 221, 318, 452, 454, 35, 202, 127, 234, 129, 233, 428, 502, 417, 472, 245, 491, 396, 64, 277, 259, 114, 30, 455, 271, 183, 358, 171, 309, 366, 88, 35, 112, 94, 135], [268, 179, 137, 341, 379, 113, 338, 78, 112, 394, 6, 336, 244, 241, 425, 438, 89, 87, 493, 171, 445, 399, 269, 18, 506, 252, 310, 452, 499, 361, 252, 343, 138, 240, 246, 477, 99, 463, 57, 153, 482, 72, 22, 318, 504, 20, 374, 62, 119, 370, 23, 369, 172, 228, 91, 289, 19, 405, 183, 152, 281, 26, 151, 188, 207, 81, 9, 68, 249, 199, 234, 316, 19, 70, 157, 317, 286, 310, 93, 426, 57, 149, 34, 156, 279, 407, 131, 359, 86, 430, 272, 169, 387, 102, 489, 227, 467, 445, 382, 118, 91, 42, 120, 328, 505, 0, 181, 451, 225, 216, 303, 424, 32, 141, 180, 315, 145, 287, 499, 111, 315, 411, 416, 380, 126, 228, 346, 10], [124, 480, 127, 192, 138, 285, 126, 327, 230, 85, 171, 295, 461, 195, 140, 289, 386, 59, 261, 453, 403, 194, 12, 511, 95, 122, 193, 213, 265, 70, 55, 372, 428, 392, 409, 219, 476, 113, 264, 279, 475, 259, 297, 458, 345, 49, 161, 314, 312, 49, 130, 48, 16, 240, 502, 294, 186, 276, 267, 290, 278, 107, 18, 453, 213, 69, 209, 214, 52, 175, 142, 236, 164, 489, 334, 125, 420, 195, 16, 16, 185, 333, 478, 305, 1, 504, 240, 248, 36, 411, 479, 260, 222, 422, 116, 273, 459,

165, 59, 164, 35, 220, 446, 131, 492, 485, 326, 34, 297, 62, 257, 56, 64, 190, 302, 434, 402, 80, 224, 294, 226, 180, 243, 510, 299, 329, 78, 293], [254, 411, 419, 227, 475, 360, 107, 381, 346, 48, 67, 53, 45, 426, 322, 6, 102, 179, 403, 443, 394, 455, 102, 406, 2, 289, 228, 417, 133, 66, 211, 338, 96, 65, 343, 157, 244, 432, 71, 6, 377, 6, 10, 473, 146, 20, 367, 0, 204, 391, 46, 321, 410, 501, 298, 167, 231, 328, 414, 422, 460, 473, 320, 143, 435, 433, 479, 316, 46, 472, 62, 441, 332, 149, 92, 309, 159, 151, 469, 150, 482, 29, 342, 344, 376, 363, 73, 64, 353, 141, 263, 336, 367, 248, 22, 90, 487, 83, 261, 273, 425, 297, 432, 200, 15, 308, 380, 372, 177, 134, 507, 204, 307, 493, 257, 195, 252, 400, 280, 110, 240, 141, 83, 269, 108, 81, 195, 249], [173, 160, 489, 196, 177, 147, 289, 131, 68, 197, 221, 468, 436, 334, 84, 242, 458, 490, 388, 304, 167, 85, 323, 248, 264, 170, 186, 456, 482, 376, 101, 191, 345, 184, 482, 477, 142, 112, 145, 105, 215, 267, 338, 283, 7, 244, 126, 404, 153, 98, 188, 285, 491, 323, 91, 173, 428, 253, 69, 284, 138, 311, 509, 420, 434, 313, 16, 287, 460, 215, 364, 364, 180, 425, 203, 121, 267, 198, 308, 399, 503, 250, 204, 479, 351, 256, 35, 94, 227, 391, 20, 261, 262, 491, 122, 99, 75, 54, 467, 352, 348, 94, 285, 296, 221, 446, 7, 194, 29, 280, 500, 266, 253, 247, 84, 398, 197, 79, 76, 65, 306, 97, 25, 268, 483, 280, 148, 88], [352, 205, 226, 154, 91, 83, 147, 425, 452, 23, 498, 257, 292, 426, 438, 472, 151, 343, 129, 92, 192, 358, 366, 62, 10, 313, 382, 280, 83, 244, 77, 214, 402, 167, 457, 275, 436, 39, 160, 114, 338, 192, 283, 402, 477, 254, 89, 355, 412, 472, 270, 504, 351, 452, 296, 129, 259, 266, 376, 296, 54, 436, 347, 458, 434, 189, 400, 107, 434, 503, 133, 382, 204, 477, 25, 30, 352, 436, 248, 8, 470, 328, 335, 281, 450, 359, 191, 364, 85, 475, 497, 170, 100, 442, 102, 358, 325, 165, 128, 264, 457, 215, 245, 287, 71, 253, 354, 185, 238, 132, 244, 321, 125, 412, 160, 414, 484, 368, 352, 65, 410, 502, 172, 300, 417, 396, 510, 416], 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133, 459, 465, 267, 188, 163, 158, 129, 100, 151, 355, 413, 18, 146, 226, 184, 310, 40, 340, 389, 206, 231, 31, 104, 275, 138, 195, 113, 304, 321, 42, 247, 66, 239, 255, 398, 360, 184, 441, 108, 206, 151, 370, 363, 112, 162, 125, 481, 106], [271, 450, 447, 370, 422, 112, 232, 81, 290, 329, 413, 10, 150, 62, 179, 60, 414, 449, 326, 126, 258, 332, 125, 59, 119, 226, 153, 182, 130, 402, 303, 70, 121, 291, 217, 10, 60, 347, 60, 403, 301, 235, 280, 226, 377, 285, 405, 292, 147, 343, 308, 455, 350, 143, 312, 443, 495, 477, 410, 438, 166, 219, 381, 187, 505, 13, 35, 266, 415, 474, 44, 396, 225, 147, 324, 73, 298, 118, 127, 219, 281, 476, 107, 390, 167, 431, 358, 441, 247, 9, 14, 76, 205, 3, 504, 390, 59, 495, 511, 58, 186, 446, 354, 92, 114, 121, 303, 287, 272, 219, 412, 336, 416, 343, 383, 356, 391, 79, 274, 363, 76, 472, 458, 358, 142, 52, 165, 469], [219, 210, 274, 470, 98, 315, 352, 328, 161, 501, 361, 284, 348, 509, 474, 397, 276, 212, 0, 200, 419, 50, 274, 446, 45, 86, 482, 166, 149, 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```

```
W=matrix(ZZ,ma)
```

```
cc= vector(ZZ,res)
```

```
# Babai's Nearest Plane algorithm
```

```
def Babai_closest_vector(M, G, target):
```

```
    small = target
```

```
    for _ in xrange(5):
```

```
        for i in reversed(range(M.nrows())):
```

```
            c = ((small * G[i]) / (G[i] * G[i])).round()
```

```
            small -= M[i] * c
```

```
    return target - small
```

```
A1=matrix.identity(42)
```

```
Ap=matrix.identity(128)*2129
B=block_matrix([[Ap],[W]])
lattice = IntegerLattice(B, llr_reduce=True)
print("LLL done")
gram = lattice.reduced_basis.gram_schmidt()[0]
target = vector(ZZ, res)
re = Babai_closest_vector(lattice.reduced_basis, gram, target)
print("Closest Vector: {}".format(re))
R = IntegerModRing(prime)
M = Matrix(R, ma)
M=M.transpose()
ingredients = M.solve_right(re)
print("Ingredients: {}".format(ingredients))
m=""
for i in range(len(ingredients)):
    m+=chr(ingredients[i])
print m
blowfishgame
(第二天没打，直接搬运)
WriteUp by Nu1L
#!/usr/bin/env python
# -*- coding: utf-8 -*-
from pwn import *
import base64
import re
from hashlib import sha384
from itertools import product
LOCAL = 0
VERBOSE = 0
if VERBOSE:
    context.log_level = 'debug'
```

```
if LOCAL:
io = process(['python2', 'blowfishgame.py'])
else:
io = remote('8.131.69.237', 15846)
table = string.ascii_letters + string.digits
# passPoW
io.recvuntil('sha384')
rec = io.recvline().decode()
suffix = re.findall(r'\(XXX\+(.*?)\)', rec)[0]
digest = re.findall(r'=(.*?)\n', rec)[0]
print("suffix: {suffix} \ndigest: {digest}")
print('Calculating hash...')
for i in product(table, repeat=3):
prefix = ".join(i)
guess = prefix + suffix
if sha384(guess.encode()).hexdigest() == digest:
print(guess)
break
io.sendlineafter(b'Give me XXX:', prefix.encode())
io.recvuntil(',_|\n\n')
p0 = b'Blowfish_w0rld'
c0 = base64.b64decode(io.recvline().strip())
sendIV, c0 = c0[:8], c0[8:]
target = b'get_flag'
iv = []
for idx, val in enumerate(target):
iv.append(sendIV[idx] ^ target[idx] ^ p0[idx])
iv = bytes(iv)
crafted_message = base64.b64encode(iv+c0)
flag = "
for boff in range(0, 48, 8):
```

```
for off in range(7, -1, -1):
    io.sendline(crafted_message)
    io.sendline("\x00"*off)
    res = base64.b64decode(io.recvline())
    target = res[boff:boff+8]
    for i in range(33, 128):
        io.sendline(crafted_message)
        io.sendline("\x00"*off+flag+chr(i))
        res = base64.b64decode(io.recvline())[boff:boff+8]
        if res == target:
            flag += chr(i)
    print(flag)
```